## M.C.A. DEGREE EXAMINATION - COMPUTER APPLICATIONS

FOURTH SEMESTER - APRIL 2016
CA 4808-RESOURCE MANAGEMENT TECHNIQUES

Date: 18-04-2016
Time: 09:00-12:00
$\square$ Max. : 100 Marks

## PART A

## Answer ALL Questions

1. In simplex method, what is the condition that a 1.p.p has infeasible solution?
2. Define the following: i. Feasible solution ii. Optimal solution.
3. Give mathematical formulation of Transportation Problem
4. State True or False
i. In Transportation Problem, VAM is more efficient than North - West Corner rule.
ii. For a balanced transportation Problem, no. of rows need not be equal to no. of columns.
5. What do you mean by decision making under conditions of uncertainty?
6. In game theory, what is saddle point?
7. What is dummy activity?
8. Define the terms: i. Total Float ii. Independent Float.
9. What is queue discipline?

10 . What is traffic intensity?

## PART B

## Answer ALL Questions

11a. Solve graphically the following 1.p.p
Maximize $Z=4 x_{1}-3 x_{2}$
Subject to $5 \mathrm{x}_{1}+3 \mathrm{x}_{2} \leq 15$

$$
\begin{gather*}
\mathrm{x}_{1}+3 \mathrm{x}_{2} \leq 6 \\
\mathrm{x}_{1}-\mathrm{x}_{2} \leq 2 \\
\mathrm{x}_{1}, \mathrm{x}_{2} \geq 0 \tag{or}
\end{gather*}
$$

11b. Solve graphically the following l.p.p
Maximize $Z=3 x_{1}-x_{2}$
Subject to $2 \mathrm{x}_{1}+\mathrm{x}_{2} \geq 2$

$$
\begin{aligned}
\mathrm{x}_{1}+3 \mathrm{x}_{2} & \leq 3 \\
\mathrm{x}_{2} & \leq 4 \\
\mathrm{x}_{1}, \mathrm{x}_{2} & \geq 0
\end{aligned}
$$

12a. A department has 4 employees with 4 jobs to be performed. The cost (in rupees) each employee will charge per hour to perform each job is given in the following matrix. How should the jobs be allocated to the employees so as to minimize the total cost.

| Employee $\rightarrow$ <br> Job $\downarrow$ | A | B | C | D |
| :--- | :--- | :--- | :--- | :--- |
| 1 | 30 | 60 | 30 | 70 |
| 2 | 50 | 40 | 65 | 70 |
| 3 | 50 | 70 | 80 | 75 |
| 4 | 40 | 80 | 55 | 70 |

(or)
12b. Describe MODI method in Transportation Problem.

13a. i. Define the terms: (a) Laplace criterion (b) Hurwicz criterion
ii. The manager of a Flower Shop purchases flowers on the previous day and delivers the customers the next day. The daily demand for roses is in the range of $70,80,90$, and 100 with respective probabilities $0.1,0.2,0.4$, and 0.3 . How many dozens of roses should the manager order to maximize the profit? The payoff matrix is given below:

| Action $\rightarrow$ <br> Event $\downarrow$ | Probability | 70 | 80 | 90 | 100 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 70 | 0.1 | 140 | 130 | 120 | 110 |
| 80 | 0.2 | 140 | 160 | 130 | 130 |
| 90 | 0.5 | 140 | 160 | 180 | 170 |
| 100 | 0.2 | 140 | 160 | 180 | 200 |

(or)
13b. Solve the game whose payoff matrix is given below:

| Player B $\rightarrow$ <br> Player $\downarrow$ | B1 | B2 | B3 | B4 |
| :--- | :--- | :--- | :--- | :--- |
| A1 | 2 | -2 | 4 | 1 |
| A2 | 6 | 1 | 12 | 3 |
| A3 | -3 | 2 | 0 | 6 |
| A4 | 2 | -3 | 7 | 1 |

14a. Given the following information

| Activity | $0-1$ | $1-2$ | $1-3$ | $2-4$ | $2-5$ | $3-4$ | $4-5$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Duration <br> (days) | 2 | 12 | 15 | 7 | 4 | 3 | 10 |

i. Draw the network diagram
ii. Identify critical path and find the total project duration.
iii. Determine total, free, and independent floats.
(or)
14b. A project consists of 7 activities. The time estimate are in days.

| Activity | A | B | C | D | E | F | G |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Predecessor | --- | A | A | C | B | D,E | F |
| $\mathrm{T}_{\mathrm{O}}$ | 1 | 2 | 3 | 6 | 3 | 2 | 4 |
| $\mathrm{~T}_{\mathrm{M}}$ | 4 | 5 | 3 | 9 | 6 | 8 | 4 |
| $\mathrm{~T}_{\mathrm{P}}$ | 7 | 14 | 3 | 21 | 15 | 17 | 4 |

i. Draw the PERT network diagram and find the critical path.
ii. Find the expected length of the critical path and its variance.

15a. At a one-man barber shop, customers arrive according to Poisson distribution with a mean of 5 per hour and service is exponential with mean of 10 minutes. If it is assumed that customers are willing to wait, then find the following:
i. Average number of customers in the shop and average no. of customers waiting
ii. The $\%$ of time a customer can walk in without having to wait
iii. Average waiting of a customer in the shop.

## (or)

15b. Cars arrive at a petrol pump with exponential inter-arrival times having mean $1 / 2$ minute. The attendant takes an average of $1 / 5$ minute per car to supply petrol, the service time being exponentially distributed. Determine
i. The average number of cars waiting to be served.
ii. The average number of cars in the queue and
ii. The proportion of time for which the pump attendant is idle.

## PART C

Answer any TWO Questions
16a. Solve the following linear programming problem
Minimize $Z=3 x_{1}-2 x_{2}-x_{3}$
Subject to $-x_{1}+2 x_{2}+3 x_{3} \leq 7$
$4 x_{1}-2 x_{3} \leq 12$
$3 \mathrm{x}_{1}+8 \mathrm{x}_{2}+4 \mathrm{x}_{3} \leq 10$
$\mathrm{x}_{1}, \mathrm{x}_{2}, \mathrm{x}_{3} \geq 0$
(12 marks)

16b. Obtain initial allocation using VAM for the following:
(8 marks)

| Destination $\rightarrow$ <br> Source $\downarrow$ | D1 | D2 | D3 | Supply |
| :--- | :--- | :--- | :--- | :--- |
| S1 | 50 | 30 | 220 | 1 |
| S2 | 90 | 45 | 170 | 3 |
| S3 | 250 | 200 | 50 | 4 |
| Requirement | 4 | 2 | 2 |  |

17a. A company has 4 salesmen A, B, C and D. These salesmen are to be allotted 4 districts $1,2,3$, and 4 . The estimated profit per day for each salesman in each district is given in the following table.

| Districts $\rightarrow$ <br> Salesmen $\downarrow$ | 1 | 2 | 3 | 4 |
| :--- | :--- | :--- | :--- | :--- |
| A | 16 | 10 | 14 | 11 |
| B | 14 | 11 | 15 | 15 |
| C | 15 | 15 | 13 | 12 |
| D | 13 | 12 | 14 | 15 |

What is the optimal assignment which will yield maximum profit?
(12 marks)
17b. Write the procedure for Hungarian method of solving Assignment Problem.
18a. The marketing department of a food products company worked out the payoffs in terms of yearly net profits for each of the strategies of three events (expected sales). This is represented in the following table:

| Nature of states $\rightarrow$ <br> Strategies $\downarrow$ | N1 | N2 | N3 |
| :--- | :--- | :--- | :--- |
| S1 | 70000 | 30000 | 15000 |
| S2 | 50000 | 45000 | 0 |
| S3 | 30000 | 30000 | 30000 |

Select the strategy on the basis of the following:
i. Maxmin criteria ii. Laplace criteria iii. Hurwicz criteria iv. Savage criteria.
(8 marks)
18b. A supermarket has two sales girls serving at the customers. The customers arrive in a Poisson fashion at the rate of 12 per hour. The service time for each customer is exponential distribution with mean 6 minutes. Find
i. The probability that an arriving customer has to wait for service.
ii. The average number of customer in the system
iii. The average time spent by a customer in the supermarket
(12 marks)

