

**LOYOLA COLLEGE (AUTONOMOUS), CHENNAI – 600 034**

B.Sc. DEGREE EXAMINATION – MATHEMATICS

SIXTH SEMESTER – APRIL 2010

**MT 6604/MT 5500 - MECHANICS - II**

Date & Time: 17/04/2010 / 9:00 - 12:00 Dept. No.

Max. : 100 Marks

**PART – A**

**Answer ALL the questions:**

**(10 x 2 =20 marks)**

1. Define Centre of Gravity.
2. Where does the C.G of a uniform circular arc of radius 'a' subtending an angle  $90^\circ$  lie?
3. Write any two applications of the principle of virtual work.
4. Define span and sag of a catenary.
5. What is amplitude and frequency of a particle executing simple harmonic motion?
6. Define Simple Pendulum.
7. What are the radial and transverse components of a velocity?
8. What is the  $p$ - $r$  equation of Hyperbola?
9. What is the moment of inertia of a circular disc about a tangent line?
10. Write down the expression for angular momentum and kinetic energy of a rigid body rotating about a fixed axis.

**PART – B**

**Answer any FIVE questions:**

**(5 x 8 = 40 marks)**

11. Find the center of gravity of a solid hemisphere.
12. Find the center of gravity of a sector of a circle of radius  $a$  subtending an angle  $2\alpha$  at the center. Deduce the center of gravity of the quadrant of the circle.
13. A solid hemisphere is supported by a string fixed to a point A on its rim and to a point O on a smooth vertical wall with which a curved surface of the sphere is in contact at P. If  $\theta$  and  $\varphi$  are the inclinations of the string and the plane base of the hemisphere to the vertical, prove that  $\tan \varphi = \frac{3}{8} + \tan \theta$ .
14. Derive the equation of the common catenary in the form  $y = C \cosh x/c$ .
15. A string 10 cms long can just support a mass of 20 gms. A mass of 3 gms is attached at one end and the other end is kept fixed. If the mass revolves uniformly in a horizontal circle, find the greatest number of revolutions it can make per second.

**(P.T.O.)**

16. A second pendulum is carried down with a lift at a uniform acceleration of  $20 \text{ cm/sec}^2$ . How many seconds an hour will it lose?
17. Derive the differential equation of the central orbit in polar co-ordinates.
18. Find the moment of inertia of the right solid cone of height  $h$  and semi-vertical angle  $\alpha$  about its axis.

### PART – C

**Answer any TWO questions:**

**(2 x 20 = 40 marks)**

19. (a) A square hole is punched out of a circular lamina of a radius 'a' having a radius as its diagonal. Show that the centre of gravity of the remaining is at a distance  $\frac{a}{4\pi - a}$  from the center of the circle.
- (b) Four rods, each of length  $a$  and weight  $W$  are smoothly joined together to form a rhombus  $ABCD$ , which is kept in shape by a light rod  $BD$ . The angle  $BAD$  is  $60^\circ$  and the rhombus is suspended in a vertical plane from A. Find the thrust in  $BD$ . (10 + 10)
20. (a) An endless uniform chain rests in equilibrium over a smooth pulley and is in contact with its over three quarters of the circumference. Show that the length of the free portion is  $\frac{\sqrt{2}}{\log(\sqrt{2} + 1)}$  times the radius of the pulley.
- (b) If a particle moving with S.H.M. has velocity  $u, v, w$ , when its distances from an arbitrary point in the straight line are  $a, b, c$  respectively, prove that its period  $T$  is given by the equation  $\frac{4\pi^2}{T^2} (b-c)(c-a)(a-b) = \begin{vmatrix} u^2 & v^2 & w^2 \\ a & b & c \\ 1 & 1 & 1 \end{vmatrix}$ . (10 + 10)
21. (a) A particle P describes the orbit  $r^n = a^n \cos n\theta$  under a central force, the pole being the centre. Find the law of force.
- (b) Derive the expression for the Kinetic energy of a rigid body moving in 2-dimensions. (10 + 10)
22. (a) Find the moment of inertia of a parabolic plate cut off by an ordinate at a distance  $h$  from the vertex, about the tangent at the vertex.
- (b) Find the moment of inertia of a hollow sphere about a diameter, its internal and external radii being  $b$  and  $a$ . (10 + 10)

\$\$\$\$\$\$