# LOYOLA COLLEGE (AUTONOMOUS), CHENNAI – 600 034

**B.Sc.** DEGREE EXAMINATION – MATHEMATICS

SIXTH SEMESTER - APRIL 2022

#### **UMT 6503 – MECHANICS**

Dept. No. Date: 20-06-2022 Time: 01:00 PM - 04:00 PM

#### PART - A

**Answer all Questions** 

- 1. When do you say that a body is in equilibrium?
- 2. If two forces P and Q are at right angles, find the magnitude and direction of the resultant.
- 3. State the conditions of equilibrium of three coplaner parallel forces.
- 4. Define couples.
- 5. State Newton's law of motion.
- 6. What are absolute units of force?
- 7. Define trajectory.
- 8. What is time of flight?
- 9. State theorem of Parellel Axis for moment of inertia.
- 10.State Dr. Routh's rule.

# PART – B

# (5X8=40)

# Answer any five Questions

- 11. Two forces act on a particle. If the sum and difference of the forces are at right angles to each other, show that the forces are of equal magnitude.
- 12. State and prove converse of the triangular law of forces.
- 13. Three like forces acting at the vertices of a triangle, have magnitudes proportional to the opposite sides. Show that their resultant passes through the incentre of the triangle.
- 14. State and prove like parallel forces theorem
- 15. A mass of 20kg falls 500cms from rest and then penetrates to a depth of 50 cm. into the sand before coming to rest. Find the average thrust of the sand.
- 16. Explain Atwood's Machine.
- 17. A stone is thrown with a velocity of 39.2 m/sec. at  $30^{\circ}$  to the horizontal. Find at what times it will be at a height of 14.7m.
- 18. Find the moment of inertia of uniform rectangular parallelepiped of edges2a, 2b, 2c.

(10X2 = 20)

Max.: 100 Marks

#### PART – C

#### Answer any two Questions

19.(a) The resultant of two forces P,Q acting at a certain angle is X and that of P,R acting at the same angle is also X. The resultant of Q,R again acting at the same angle is Y. Prove that  $P = (X^2 + QR)^{1/2} = \frac{QR(Q+R)}{Q^2+R^2-Y^2}$ . If P+Q+R =0 show that Y=X.

(b)ABCDEF is a regular hexagon and at A, act forces represented by  $\overline{AB}$ ,  $2\overline{AC}$ ,  $3\overline{AD}$ ,  $4\overline{AE}$  and  $5\overline{AF}$ . Show that the magnitude of the resultant is AB $\sqrt{351}$  and that it makes an angle  $\tan^{-1}(\frac{7}{\sqrt{3}})$  with AB.

20. (a) Show that when masses P and Q are connected by a string passing over the edge of a smooth table, the tension is the same whether P hangs and Q is on the table or Q hangs and P is on the table.

(b) Two particles of masses  $m_1$  and  $m_2$  are connected by a light inextensible string passing over a light smooth pulley placed at the top of a smooth inclined plane of inclination  $\alpha$  to the horizon ,  $m_1$  is hanging freely and  $m_2$  is lying on the inclined plane the portion of the string on the inclined plane being parallel to the inclined plane. If  $m_1$ descends, find the resulting motion and the tension in the string.

21. (a) A particle is thrown over a triangle from one end of a horizontal base and grazing the vertex falls on the other end of the base. If A and B are the base angles and  $\alpha$  the angle of projection, show that tan  $\alpha$  = tan A + tan B.

(b) The range of a rifle bullet is 1000m when a is the angle of projection. Show that if the bullet is fired with the same elevation from a car travelling 36km/h towards the target, the range will be increased by  $\frac{1000\sqrt{\tan \alpha}}{7}$  m.

22(a) Find the M.I. for the uniform elliptic lamina.

(b) Show that the moment of inertia of a triangular lamina of mass M about a side is  $\frac{Mh^2}{6}$  where h is the altitude from the opposite vertex.