## LOYOLA COLLEGE (AUTONOMOUS), CHENNAI - 600034

B.Sc. DEGREE EXAMINATION - PHYSICS

THIRD SEMESTER - NOVEMBER 2022
UPH 3502 - MATHEMATICAL PHYSICS - II

Date: 03-12-2022
Time: 09:00 AM - 12:00 NOON

## PART - A

Q. No. Answer ALL questions
( $10 \times 2=20$ Marks)
1 Distinguish between ordinary and partial differential equations.
2 Find the general solution of the differential equation $\left(D^{\prime \prime}+16\right) y=0$.
3 Solve the differential equation $\frac{\partial^{2} u}{\partial y^{2}}=0$.
4 Write the Laplacian equation in cylindrical coordinates.
5 State the derivative property of Fourier's transform.
$6 \quad$ Find the Fourier transform of $f(x)=\left\{\begin{array}{l}1, \text { for }|x|<a \\ 0, \text { for }|x|>a\end{array}\right.$
7 Write the Newton's backward interpolation formula.
8 What is meant by interpolation?
9 Using Newton-Raphson formula find the square root of a positive number k .
10 Write the Lagrange's interpolation formula.

## PART - B

## Answer any FOUR questions

11 Using the method of separation of variables, solve $\frac{\partial u}{\partial x}=2 \frac{\partial u}{\partial t}+u$, where $u(x, 0)=6 e^{-3 x}$.
12 Analyze the D'Alembert's solution of wave equation $\frac{\partial^{2} u}{\partial x^{2}}=\frac{1}{c^{2}} \frac{\partial^{2} u}{\partial t^{2}}$.
13 Find the Fourier sine and cosine transforms for $f(x)=e^{-2 x}+4 e^{-3 x}$.
14 State and prove convolution theorem of Fourier series.
15 Find the positive root of $x^{4}-x=10$ and correct to three decimal places using Newton's Raphson method.

16 Fit a straight line to the following data using the least square method

| $x$ | 1 | 2 | 3 | 4 |
| :--- | :--- | :--- | :--- | :--- |
| $y$ | 16 | 19 | 23 | 26 |

## PART - C

Answer any FOUR question
17 Solve the wave equation $\frac{\partial^{2} u}{\partial t^{2}}=a^{2} \frac{\partial^{2} u}{\partial x^{2}}$ for the boundary condition $\mathrm{u}=0$ when $\mathrm{x}=0$ and $\mathrm{x}=\pi$, $\frac{\partial u}{\partial t}=0$ when $t=0$ and $u(x, 0)=x, 0<x<\pi$
18 Solve $\frac{\partial^{2} u}{\partial r^{2}}+\frac{1}{r} \frac{\partial u}{\partial r}+\frac{1}{r^{2}} \frac{\partial^{2} u}{\partial \theta^{2}}=0$ by the method of separation of variables.
19 Write the one-dimensional heat equation and derive its general solution.
20 Find the Fourier transform of the function

$$
f(x)=\left\{\begin{array}{ccc}
1-x^{2} \text { if } & |x| \leq 1 \\
0 & \text { if } & |x|>1
\end{array}\right.
$$

21 The population of a city in census taken once in 10 years is given below. Estimate the population in the year 1956. (Use Newton's forward interpolation)

| Year | 1951 | 1961 | 1971 | 1981 |
| :--- | :--- | :--- | :--- | :--- |
| Population in thousands | 35 | 42 | 58 | 84 |

22 Evaluate $\int_{-3}^{3} x^{4} d x$ using Trapezoidal rule and Simpson's one third rule. Verify your answer with actual integration.

